# Temporal Graph Mining for Fraud Detection

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*Abstract*— Given interacting entities (customers buying products; Twitter users re-tweeting posts; patients visiting doctors; machines sending packets to machines), how can we spot anomalies and possibly fraud? What should we do if we know that some entities are fraudulent?

The problem has attracted huge interest; several suspicious patterns have been discovered, and several tools to spot such patterns have been developed. We survey the most successful, time-tested tools, starting with classic ones (matrix factorization, belief propagation, dense block detection) and continuing with newer, equally successful ones, and specifically multi-relational learning, and graph neural networks GNNs.

Focusing on practitioners, we also present some past success stories from diverse settings (phonecall networks, online retailers, social networks); we list some types of fraud and their tell-tale signs; and we also list the node-features that we found most useful (degree, core-number, etc), as well as some graph-visualization tools.

Index Terms—graph mining, fraud detection, visualization, time-evolving

## I. RATIONALE

Finding patterns and anomalies in graphs has numerous applications: in social networks, users may be re-tweeting posts after being paid to do so; in health-insurance fraud, patients collude with doctors to file fraudulent claims; in computer network security, machines sending packets to machines for a DDoS attack, and numerous more. The tutorial presents an organized list of time-tested tools, as well as fraud M.O.s (modus operandi), with emphasis on the intuition behind each tool and its applicability to real settings.

See section IV for relevance, and section VI for differences from earlier tutorials.

## II. CONTENT DETAILS

- 1) [5'] Introduction and Motivation. [Fidalgo]
- 2) [10'] Types of fraud 'behind enemy lines' [Fidalgo]
  - a) in online retailers (Alibaba: brushing)
  - b) in fake reviews (Flipkart)
  - c) in Twitter (sock-puppets; reciprocity)
  - d) in Facebook (synchronized behavior)
  - e) in Weibo (sync, again)

Thanks to the AIDA project (OCI-01-0247-FEDER-045907), co-funded by ERDF, COMPETE 2020 and FCT under CMU Portugal, and the São Paulo Research Foundation (FAPESP, grants No. 2016/17078-0, 2021/11403-5, 2020/11258-2).

- f) in phone networks (wan-giri, int-rev-share, int-bypass, camouflage; 'bridge' nodes from Pedro F.)
- g) in crypto (Srijan++)
- 3) [25'] Static Graphs unsupervised [Faloutsos]
  - a) Patterns (degree distribution, conn. components, etc) Graph Mining book (Chakrabarti and Faloutsos) [1],
  - b) Node Importance, Node Proximity, Link Prediction: SVD, PageRank [2], HITS [3], SALSA [4],
  - c) Tools OddBall [5], CopyCatch [6], EigenSpokes [7], Fraudar [8]; Survey on anomaly detection [9]
  - d) Communities/clusters METIS [10], Coclustering [11], Cross-associations [12])
- 4) [10'] Static Graphs semi-supervised [Faloutsos]
  - a) Featureless nodes: Belief propagation [13] and variants (FastBP [14] zooBP [15], [16])
  - b) Applications/Success stories: NetProbe [17], Snare [18], Polonium [19].
- 5) [10'] Time evolving graphs [Faloutsos]
  - a) Patterns: spikeM [20], RSC [21], [22]
  - b) Tools (tensors [23], timeCrunch [24] ) AnomRank [25] SpotLight [26]
- 6) [15'] General tools for outlier / micro-cluster detection [Faloutsos]
  - a) Isolation Forest [27] and gen2Out [28]
  - b) and many more: LOF [29]; LOCI [30]
  - c) Even standard clustering methods: DBSCAN/OPTICS [31], [32]
- 7) [5'] List of node-features (ever-growing) [Cazzolato]
  - a) degree (in/out); weighted; unique-degree
  - b) core#
  - c) Inter-arrival time IAT (median, mad, quantiles)
- 8) [10'] Visualization tools [*Cazzolato*]
  - a) Apring model [33]
  - b) Adjacency matrix (after re-ordering) [34]
  - c) 1-d distributions (pdf / ccdf / odds-ratio, in log-log)
  - d) Scatter-plots / pair-plots (lookout) [35]
  - e) Parallel axis [36]
  - f) Demo of TgraphSpot from GitHub
- 9) [5'] Conclusions [Cazzolato]

## III. TARGET AUDIENCE

*Intended audience*: Data scientists and practitioners, working on anomaly and fraud detection on large static and timeevolving graphs. *Prerequisites*: freshman matrix algebra (matrix multiplication, definition of eigenvalues), basic probability.

# IV. RELEVANCE AND RATIONALE

See section I for the rationale.

## V. LIST OF FORUMS

This is the first time we offer this tutorial. Some parts of it (static patterns, outline item 3, and semi-supervised methods, outline item 4) have been presented in graph mining tutorials (KDD17, WSDM13 - see below for the differences).

#### VI. LIST OF PAST TUTORIALS

- WSDM 2013 tutorial (*Anomaly, Event, and Fraud Detection in Large Graph Datasets*) proposal - and website with lecture slides. This is 10-year-ago tutorial - we have added recent material and recent papers.
- KDD 2017 tutorial (*Data Driven Approaches towards Malicious Behavior Modeling*) (slides). There was more emphasis on behavior modeling than graph mining and feature extraction.

# VII. TUTORS BIOS

*Christos Faloutsos:* is a Professor at Carnegie Mellon University. He has received the Presidential Young Investigator Award by the National Science Foundation (1989), the Research Contributions Award in ICDM 2006, the SIGKDD Innovations Award (2010), the PAKDD Distinguished Contributions Award (2018), 31 "best paper" awards (including 8 "test of time" awards). He has given over 50 tutorials and over 25 invited distinguished lectures. His research interests include large-scale data mining with emphasis on graphs and time sequences; anomaly detection, tensors, and fractals.

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#### VIII. PROPOSED LENGTH

2.5 hours.

# IX. SLIDES/NOTES/VIDEOS

- Faloutsos: website with lecture slides; and keynote talk (York Univ., 2016)
- Cazzolato: TgraphSpot Presentation (BigData 2022); and TgrApp Demo Presentation (AAAI 2023);
- Fidalgo, Faloutsos, Cazzolato: AIDA Webinar.

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